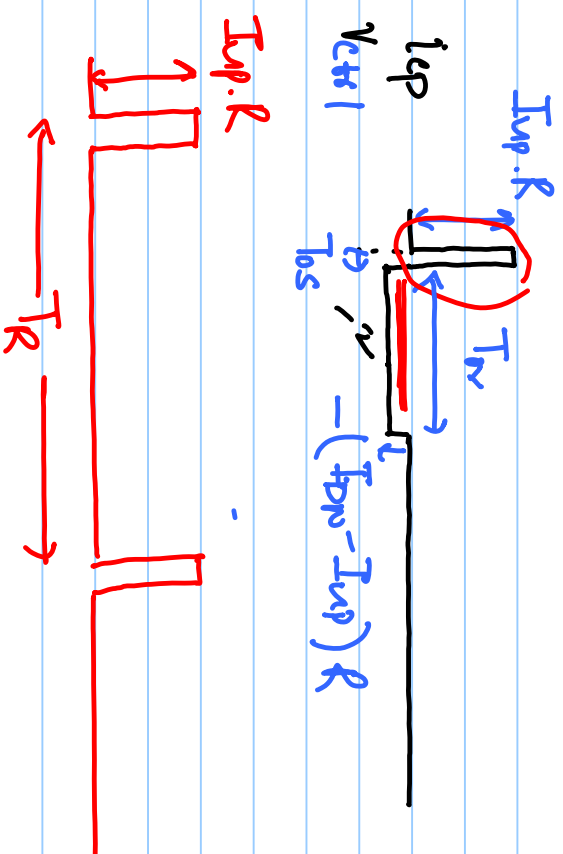
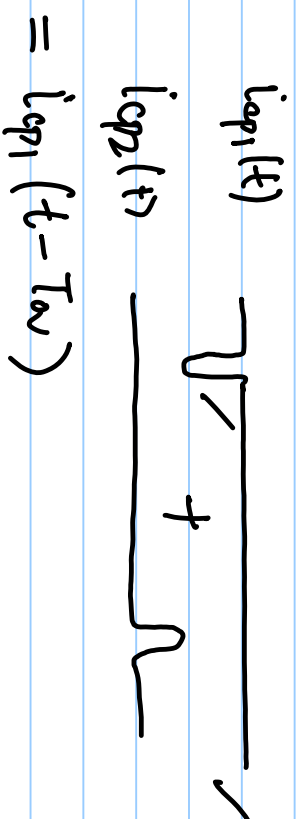


Charge-pump



$$V_{\text{cell}} = a_0 + \sum a_n \cos(n\omega_p t) + b_n \sin(n\omega_p t)$$

$$\int_0^{T_0} \sin \omega t \cos(m\omega t) dt = \frac{1}{2} \int_0^{T_0} \cos^2(m\omega t) dt$$

$$\frac{I_{up} \cdot R}{m \omega_R} \sin(m \omega_R t) \Big|_0^{T_{os}} = \frac{a_m}{2} \int_0^{T_R} 1 - \cos(2m \omega_R t) dt$$

$$\frac{I_{up} \cdot R}{m \omega_R} \sin(m \omega_R \cdot T_{os}) = \frac{a_m}{2} \cdot T_R$$

$$a_m = \frac{2}{T_R} \frac{I_{up} \cdot R}{m \omega_R} \sin\left(m \cdot \frac{2\pi}{T_R} \cdot T_{os}\right)$$

$$a_m = \frac{1}{m\pi} \cdot \frac{2\pi}{T_R} I_{up} \cdot R \sin(m \cdot \frac{2\pi}{T_R} \cdot T_{os}) \quad \checkmark \Rightarrow a_1 = \frac{I_{up} \cdot R}{\pi} \sin(\Phi_{os})$$

$$\frac{I_{up} \cdot R}{m \omega_R} \cos(m \omega_R t) \Big|_0^{T_{os}} = \frac{b_m}{2} \int_0^{T_R} 1 + \cos(2m \omega_R t) \cdot dt$$

$$\frac{I_{up} \cdot R}{m \omega_R} [1 - \cos(m \omega_R T_{os})] = \frac{b_m}{2} \cdot T_R$$

$$b_m = \frac{1}{m \pi} I_{up} \cdot R [1 - \cos(m \omega_R T_{os})]$$

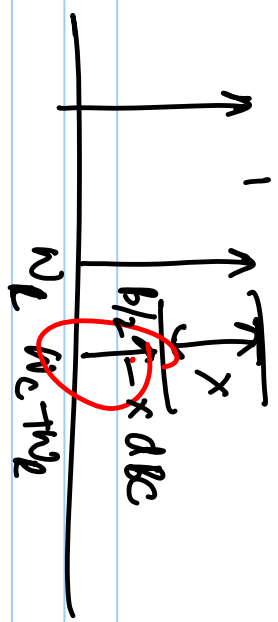
$$V_{cr1} = V_{cr10} + a_0 + a_1 \cos(\omega_R t)$$

$$f_{vco} = K_{vco} (V_{cr10} + a_0) + K_{vco} a_1 \cos(\omega_R t)$$

$$V_{out} = \sin\left(2\pi K_{vco} (V_{cr10} + a_0)t + \int 2\pi K_{vco} a_1 \cos(\omega_R t) dt\right) \\ = \sin\left(\omega_0 t + \frac{2\pi K_{vco} a_1}{\omega_R} \sin(\omega_R b)\right)$$

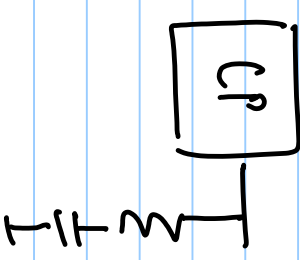
$$\beta = \frac{2\pi K_{vco}}{\omega_R} a_1 = \underbrace{\frac{2\pi K_{vco}}{\omega_R}}_{\beta} \cdot \frac{I_{up} \cdot R}{\pi} \sin(\phi_{os})$$

$$\text{Ref. Spur} = +20 \log_{10} \left(\frac{2\sqrt{K_{vco}} \cdot I_{up} \cdot R}{\omega_R \cdot \cancel{f_R}} \sin(\underline{\phi}_{os}) \right)$$

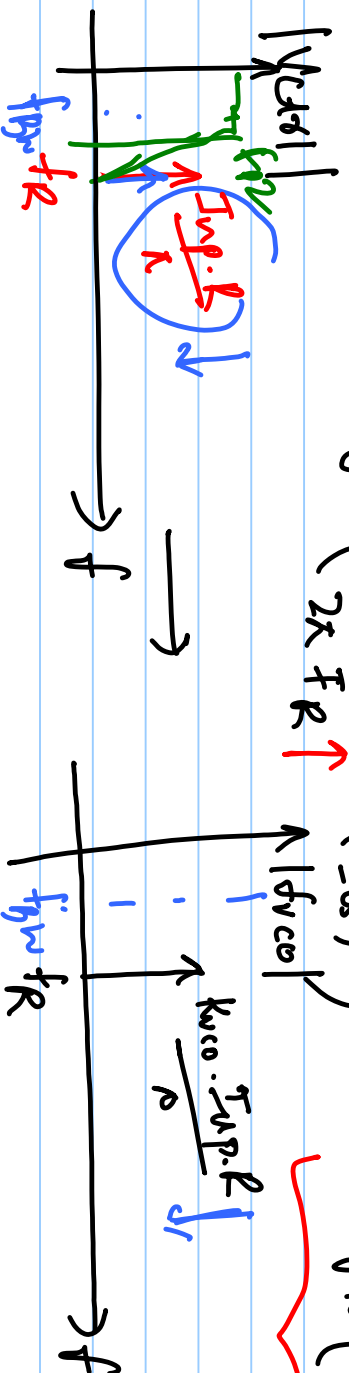


$$= 20 \log_{10} \left(\frac{\text{Mag. of Spur}}{\text{Mag. of carrier}} \right)$$

$$= 20 \log_{10} \left(\frac{K_{vco} \cdot I_{up} R}{\omega_R} \sin(\underline{\phi}_{os}) \right)$$

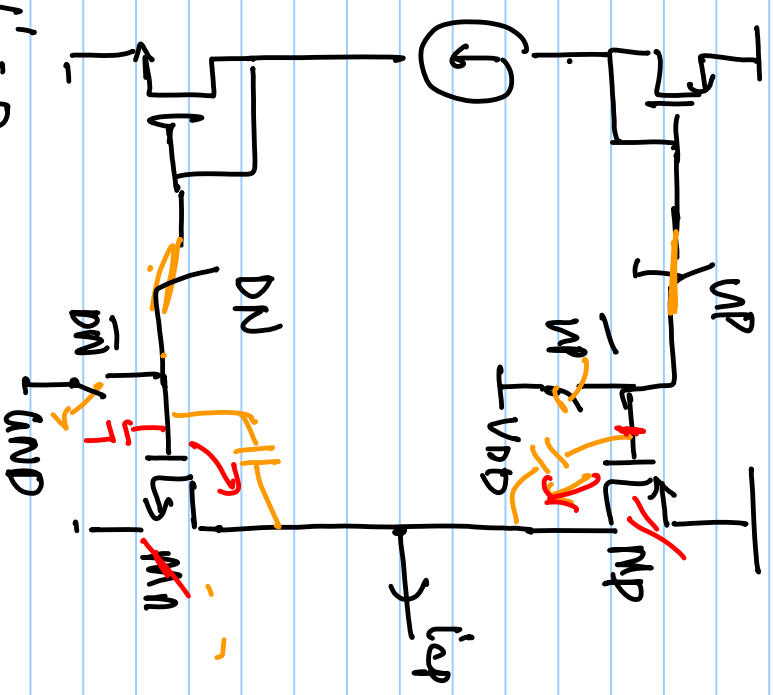
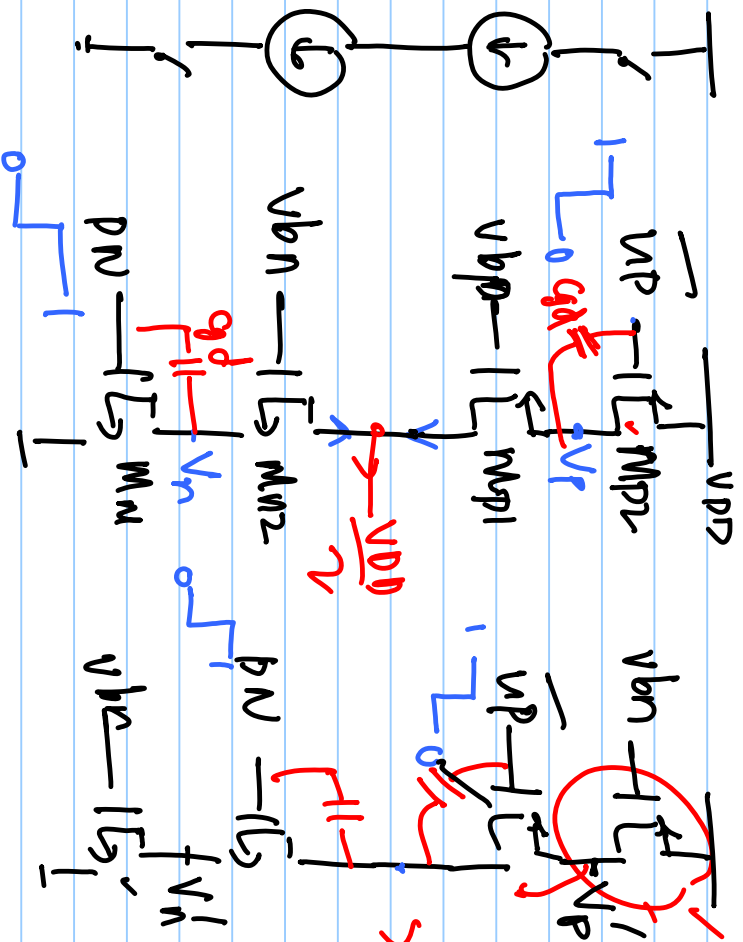


$$= 20 \log_{10} \left(\frac{f_{BW} \downarrow}{2\pi f_R \uparrow} \sin(\underline{\phi}_{os}) \right) + 20 \log_{10} \left(\frac{f_{12} \downarrow}{f_R} \right)$$



Source-switched

Drain-switched



OFF state: $V_n = V_{bn} - V_{tp}$

$$V_p = V_{bp} + |V_{tn}|$$

ON state: $V_n = 0$

$$V_p = V_{bp}$$

OFF state: $V_n' = 0$

$$V_p' = V_{DD}$$

ON state: $V_n' =$

$$V_p' =$$

